Government policy and the dynamics of market structure: Evidence from Critical Access Hospitals

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Abstract

Many government policies either target the underlying supply infrastructure or have indirect effects on market structure. In this paper we seek to understand the impact of the Critical Access Hospital (CAH) program on the U.S. rural hospital infrastructure and societal welfare. This program provides generous reimbursement to hospitals in exchange for size and service limitations. We specify and estimate a model of the rural hospital industry in which hospitals choose investment, exit and conversion to CAH status. Because these choices have dynamic impacts and even rural hospitals have geographically close competitors, we model hospitals as a dynamic oligopoly. We estimate the structural parameters from this model using a two-step inference method and assess the structural and welfare impacts of the CAH program. Our methods extend current estimation techniques for dynamic oligopoly models to allow for investment behaviors that are more consistent with observed data. Our estimated parameters on investment costs and the costs of CAH conversion appear reasonable in magnitude. Preliminary results reveal that the CAH program increases the decreases exits by 6% but also decreases consumer welfare.

Keywords: Hospitals, Exits, Dynamic Oligopoly, Medicare.

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1 Introduction

Governments often enact policies that target the underlying supply infrastructure, either directly or indirectly. Examples abound and span countries and industries. Agricultural price supports impact the number and size distributions of farms. Education vouchers and the Charter school option affect the number and size distribution of private schools. Given the magnitude of these supports the welfare consequences of these programs are likely large. However, assessing the impact of these programs on welfare and other outcomes is often a difficult task. These programs affect the returns to market participation; thus their impact will be a direct consequence of entry, exit and investment decisions by a potentially large number of organizations. Assessing the impact of these programs requires measuring the impact on dynamic equilibrium outcomes (both discrete and continuous) of forward-looking agents. Until recently the estimation of the underlying “deep” parameters necessary to calculate the impact of these programs on industry market structure was computationally burdensome. However, recent advances in the estimation of dynamic games has made such estimation feasible.

In this paper we seek to understand the impact of the Critical Access Hospital (CAH) program on the U.S. rural hospital infrastructure and societal welfare. The overarching purpose of this program is to improve the access to care of the rural population by keeping open hospitals that would otherwise close. The CAH initiative is a voluntary program in which hospitals limit their capacity, measured by beds, and services to proscribed levels. In return for participating, hospitals opt out of the standard Prospective Payment System (PPS) and receive cost-based reimbursements from the Medicare program. These payments are generally significantly more generous than what the hospital would earn under PPS. Since the 1997 implementation of the program, over 1,100 rural hospitals (roughly 25% of all US hospitals) have converted to CAH status. CAH status also dramatically reduced the capacity of rural hospitals. In 2006, CAH hospitals were expected to receive $5 billion in cost-based reimbursements, $1.3 billion more than what they would have received under PPS (MedPAC 2005). This large scale suggests that an evaluation of the CAH program is
intrinsically important. Moreover, such an evaluation can also inform us about the welfare impacts and hidden costs of the CAH program, and how the compare to alternate programs.

To evaluate the impact of the CAH program, we estimate a dynamic model of rural hospital exit, investment and CAH status.\(^1\) Each period, hospitals endogenously select their size (as measured by number of beds), decide whether to exit and post-1997 select whether or not to invest in becoming a CAH. Firms face stochastic and varying investment costs, which generates randomness in the outcomes of the model. Following the dynamic decisions, hospitals engage in static production, choosing prices for non-Medicare patients. Individuals then fall ill and decide at which hospital to seek treatment. They make their decisions based on their distance to each hospital, their own diagnosis, and characteristics of the hospital, such as beds. Hospitals seek to maximize an objective function that includes both profits, volume and the provision of service, in the case of not-for-profit and government hospitals. The decisions are made in dynamic equilibrium, where hospitals take account of the effect of their investment and conversion decisions on other hospitals in their market. Our model is a function of unknown parameters that pertain to the objective function for not-for-profits, the cost function for investing or disinvesting in beds, the costs of obtaining CAH status and the static returns given a particular state.

To estimate the dynamic parameters of the model, we build upon the approach of Bajari et al. (2007) (henceforth BBL). BBL’s insight is that competitors’ observed strategies can be used in place of equilibrium behavior, thereby averting the computational burden of solving for the equilibrium of the game for every evaluation of the parameter vector.\(^2\) Pakes et al. (2007), Aguirregabiria and Mira (2007) and Pesendorfer and Schmidt-Dengler (2007) have also suggested approaches to estimate parameters of dynamic games that rely on similar ideas. We develop a version of the BBL algorithm that allows for private information in the investment process consistent with our model. The estimation algorithm allows us to recover the dynamic parameters noted above. Separately, we estimate static profits using data on revenues and costs and estimate consumer preferences using consumer choice data.

\(^1\)Entry is rare in rural hospital markets and therefore our analysis does not consider it.

\(^2\)Hotz and Miller (1993) first proposed a similar two-step approach to estimate the parameters of a single-agent dynamic decision making process.
We then use these parameters to solve for the equilibrium and resulting welfare levels under different counterfactual policies, including having no CAH program, having different hospital size thresholds and the change to a lump-sum policy.

The remainder of this paper is divided as follows. Section 2 provides the institutional background of the CAH program. Section 3 describes our data. Our model is presented in section 4, and section 5 describes our estimation method. The results and policy experiments are presented in sections 6 and 7 respectively, and section 8 concludes.

2 The Critical Access Hospital Program

2.1 Background

The CAH program was enacted in the Balanced Budget Act (BBA) of 1997. Designated CAHs receive cost-based Medicare reimbursements for inpatient, outpatient post-acute (swing bed) and laboratory services. To qualify for the program, hospitals must be 35 miles from a primary road and 15 miles by a secondary road to the nearest hospital. However, this distance requirement can be waived if the hospital is declared a “necessary provider” by the state, and, until recently, the distance requirement does not appear to be binding. Most CAHs are less than 25 miles from a neighboring hospital. The BBA legislation stated that CAHs can only treat 15 acute inpatients and 25 total patients including patients in swing beds. A swing bed is one which can be used to provide either acute or skilled nursing facility care. In the 1997 legislation the maximum size of a hospital is 15 beds and the length of stay is limited to 4 days for all patients.

CAH hospitals are required to provide inpatient, laboratory, emergency care and radiology services. A CAH must develop agreements with an acute care hospital related to patient referral and transfer, communication, emergency and non-emergency patient transportation. The CAH may also have an agreement with their referral hospital for quality improvement

\[3\text{Much of the information in the section is culled from MedPAC (2005), which contains much more background that we provide.}\]
or choose to have that agreement with another organization. Last, the CAH legislation provides resources for hospitals to hire consultants to project revenues and costs under the CAH program and determine which strategy is best for the hospital given their objectives.

The program’s rules have been modified several times since its inception. Table 1 summarizes the important legislative and regulatory changes in the program. The most important of these changes are: 1) The Balanced Budget Reconciliation Act (BBRA) of 1999 changed the length of stay requirement and allowed states to designate hospitals in Metropolitan Statistical Areas ‘rural’ for CAH classification; 2) The Medicare Prescription Drug, Improvement and Modernization Act (MMA) of 2003 increased the acute inpatient limit from 15 to 25 acute patients and increased the payments from 100 to 101 percent of costs. Thus, there is variation in payoffs to becoming a CAH across both time and hospitals.

Figure 1 shows the rate of CAH conversion among all general acute care hospitals in the U.S. Conversion rates were very low until 1999. Starting in 1999, there is roughly a 4% conversion rate per year until the end of our sample period. We believe that the delay between the enactment of BBA in 1997 and the timing of conversion is due to the application process, which requires large amount of paperwork, inspection visits and CMS approval. By 2005, 25% of candidate hospitals have adopted CAH. It is said that conversion rates should decline after 2006, when the minimum distance requirement will be enforced (MedPAC 2005).

The spatial distribution of CAHs is shown in Figure 2. CAHs are present in most states, except New Jersey, Delaware, Rhode Island, Connecticut, and Massachusetts, which do not participate in the program. CAHs concentrate in the Midwest, and are mostly outside of MSAs.

The CAH program affects the incentives of hospitals and patients along a number of dimensions, and thus its aggregate welfare effects are unclear. Primarily, the program affects rural hospitals’ exit probabilities, keeping open hospitals that would otherwise close. Residents of rural areas may benefit from the CAH program because they would have to travel longer distances to receive medical care had the closest hospital exited the market.

For example, in the state of Wisconsin, the application process is an 18-step process, detailed at http://www.worh.org/pdfetc/AppFlowChart.pdf
This is indeed the purpose of the program. However, the impact of the CAH program on hospital prices for private pay patients is unclear and it is thought to have increased Medicare expenditures. Moreover, the program limits hospital beds and services which may harm patients, may lower the incentives of hospitals to minimize costs and may interfere with the evolutionary improvement of the industry as in Jovanovic (1982).

2.2 Previous Research

A number of studies examine hospital exit and thus relate to the CAH program. For example, Lillie-Blanton et al. (1992) and Ciliberto and Lindrooth (2007), find that smaller hospitals are more likely to close. Wedig et al. (1989) finds that for-profit hospitals are more likely to exit due to competing uses of capital. Similar conclusions are reached by Ciliberto and Lindrooth (2007) and Succi et al. (1997). Hansmann et al. (2002) consider four types of ownership and they also find that for-profit hospitals were the most responsive to reductions in demand by exiting the market, followed by public nonprofits, religiously affiliated nonprofits, and secular nonprofits responded the least. These papers have studied what determines exits, without taking into account strategic interactions, as our work does.

With respect to the effect of closures on surviving hospitals, Lindrooth et al. (2003) focused on urban hospitals and found that the costs per adjusted admission declined by 2-4% for all patients and by 6-8% for patients who would have been treated at the closed hospital. They abstract from the issues of access to care that closures generate due to their focus on urban hospitals within 5 miles from the closing one. In contrast, McNamara (1999), studies the impact of rural hospitals closures on consumers’ surplus using a discrete choice travel-cost demand model. He finds that the average compensating variation for the closure of the nearest rural hospital that makes the average shortest distance increase from 9 miles to 25 miles is about $19,500 dollars of 1988 per sample hospitalization. These papers all consider the period before 1998, before hospitals were effectively converting into CAH.

Several more recent studies examine aspects of the CAH program. Stensland et al. (2003) studies the financial effects of CAH conversion. Comparing hospitals that converted in 1999
to other small rural hospitals, they find a significant association of CAH conversion with increases in Medicare revenue, increases in hospital profit margins from -4.1% to 1.0%, and increases in costs per discharge of 17%. They state that local patients and CAH employees benefit from the improved financial conditions, but do not calculate whether the benefits are worth their cost. Stensland et al. (2004) redo their analysis for hospitals converting in 1999 and 2000, reaching similar conclusions. Casey and Moscovice (2004) studies the quality improvement initiatives of two CAHs after conversion, and conclude that the cost-based payments help the hospitals to fund activities that would improve quality of care such as additional staff, staff training and new medical equipment.

Although this literature has greatly enhanced our understanding of hospital exits and the CAH program, it does not explicitly examine the welfare impact of the CAH program. Nor does it take into account the strategic interactions between hospitals. Thus, it cannot be used to analyze the impact of CAH and of counterfactual policies for rural hospitals.

3 Data

We construct our dataset by by pooling information from various sources. Primarily, we use the publicly available Hospitals Cost Reports Information System (HCRIS) panel data set from the Centers for Medicare and Medicaid Services (CMS), years 1994-2005. Hospitals are required to file a cost report at the end of each fiscal year, where they report detailed financial and operational information needed to determine Medicare reimbursements, and this dataset contains the resulting information. For our purposes, these data report the number of beds, inpatient discharges, inpatient and outpatient revenues, salaries, and accounting information such as inpatient and outpatient costs, depreciation, asset values and profits, as well as a unique provider number assigned by CMS. Our HCRIS sample is the set of non-federal general acute care hospitals.

The information from the HCRIS was complemented with data on the timing of conversion.

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5The reporting periods for hospitals differs in length, and beginning and end dates. We created a panel with one observation per calendar year, by disaggregating the data to the quarter level and then aggregated it back to the calendar year level.
to CAH from the Flex Monitoring Team.\textsuperscript{6} When hospitals convert to CAH, a new provider number is issued by CMS, even if ownership does not change. By using data from Flex, we were able to link the new and old provider numbers, which is necessary to understand the dynamics of the industry. Using the merged data, we find that only 14 hospitals entered a particular market as a new facility, and therefore, we do not model entry. In addition, the Flex data contains accurate information on the number of beds for the hospitals that converted, which was used to verify the HCRIS information.

We link these two datasets with the American Hospital Association Annual Survey (AHA), using the CMS provider number to perform the linkage. Our primary use of the AHA data is to determine hospital latitude and longitude which we use to compute distances and markets. We also need to estimate the determinants of hospital choices. For this, we use 2003 hospital discharge data from California’s Office of Statewide Health Planning and Development (OSHPD).

We complete our hospital data with information from the Department of Health and Human Services’ Office of Inspector General’s (OIG) reports on hospital closures, years 1994-2000. These reports contain a list of the hospitals that exited the market during the year. Because the year of exit in the OIG reports differs to the last report filed for about a third of the exitors, we use the OIG information to identify exitors and we assume the hospital exits at the end of the year of their last report. After 2000 we proceed in the same fashion, but our source of data to identify closures are the Registered Deletions section from the AHA Survey, years 2001 to 2005.

We also use data from the 2000 U.S. census on residential locations. For our purposes, these data provide information on the number of people by age in each census tract.

Using the hospital data, we designate a set of hospitals that we determine are candidates for CAH conversion. Because the policy’s stated objective is to maintain access to emergency and inpatient care for rural residents we let rurality be a necessary condition for conversion.

\textsuperscript{6}The Flex Monitoring Team is a collaborative effort of the Rural Health Centers at the Universities of Minnesota, North Carolina and Southern Maine, under contract with the Office of Rural Health Policy. The Flex Monitoring Team monitors the performance of the Medicare Rural Hospital Flexibility Program (Flex Program), with one of its objectives being the improvement of the financial performance of CAH.
We characterize rurality using the Rural-Urban Commuting Area Codes (RUCA), version 2.0.\textsuperscript{7} This measure is based on the size of cities and towns and their functional relationships as identified by work commuting flows, and have been used by CMS to target other rural policies, such as the ambulance payments. CMS considers a census tract to be rural if and only if it has a RUCA greater or equal than 4, and we adopt the same criterion in this paper.\textsuperscript{8} The definitions of the RUCAs are shown in Table 2. Since only small hospitals ever convert to CAH status, we also allow only hospitals with 225 beds or less to be candidates for CAH conversion. These two criteria determine our sample for ‘at-risk’ hospitals.

We then use the location data to determine geographic markets. We first define a 150 km circle about the hospital. All hospitals in this circle, including those that are not candidates for CAH conversion, are included in the market. Hospitals that are further away have a lesser strategic impact than nearby hospitals. Potential patients are all the residents of the census tracts within the 150 km radius.

4 Model

4.1 General setup

We specify a dynamic oligopoly model of interaction between hospitals where the decisions of hospitals reflect a Markov Perfect equilibrium. This model follows in the spirit of dynamic oligopoly models developed by Ericson and Pakes (1995) and first applied to the hospital industry by Gowrisankaran and Town (1997). The specifics of our model follow more recent work on estimation of dynamic oligopoly models, such as Ryan (2006) and Collard-Wexler (2006), and build on these works by incorporating functional forms for investment that are more consistent with the data and specifics of the small hospital sector. In comparison to Gowrisankaran and Town (1997), our current work incorporates a richer model of the hospital

\textsuperscript{7}These measures are developed collaboratively by the Health Resources and Service Administration, the Office of Rural Health Policy, the Department of Agriculture’s Economic Research Service, and the WWAMI Rural Health Research Center.

\textsuperscript{8}Department of Health and Human Services, Medicare Program, Revisions to Payment Policies, etc.; Final Rule. Dec 2006.
sector – that allows for variation in geography, size and hospital characteristics – and can be estimated using recently available micro-level data and estimation techniques for dynamic models (see Bajari et al. (2007)).

The unit of observation in our model is a market, generally a rural area. At any point in time, each market contains a set of hospitals \( 1, \ldots, J_t \), who are strategic, forward-looking players. Each period, there is an identical set of consumers \( 1, \ldots, I \), who seek treatment for their illness. Hospitals are differentiated by their location, CAH status, size, ownership structure and productivity, while consumers are differentiated by their location and illness cost. Time is discrete with a period corresponding to a year and hospitals discount the future with the same discount factor \( \beta \). In our model, dynamic considerations are relevant for hospitals because hospitals’ characteristics are persistent from year to year.

We specify that any hospital with 225 beds or less located in a RUCA zip code of four or higher is a strategic player of our game. We limit our sample to these hospitals because large or urban hospitals will have different objectives, would be unlikely to qualify for CAH status, and likely do not make their decisions in response to small rural hospitals located in an area around them. Nonetheless, patients may choose these large hospitals. For instance, patients in a rural county may travel to a big-city hospital located relatively nearby to them. Indeed, regulations require CAH hospitals to develop referral agreements with a larger hospital. For this reason, we let all other hospitals in the U.S. be modeled as non-strategic players whose characteristics evolve exogenously.

Each period, we model a game with four stages. First, nature moves and provides each hospital with a period-specific investment cost shock. Second, knowing the value of their individual shocks, hospitals in the market simultaneously choose their strategies for investing in beds, exiting and obtaining CAH status. Third, hospitals choose prices for non-Medicare patients. Finally, each patient selects a hospital based on their insurance status and other characteristics. Note that we do not allow hospitals to change their locations, productivity or ownership status.

We do not model entry since entry is very rare in our data. In particular, among hospitals in our sample, 97 percent existed at the first period of our estimation, in 1998. Given this
limited amount of entry, we believe that entry is not a huge feature of this market. Of course, given that our model is dynamic, we might expect more entry in the long run, as current firms exit due to random shocks. However, it would be hard to credibly identify the parameters on the entry distribution given the paucity of entry in the data.

Hospitals make their investment, exit, CAH conversion and production decisions in order to maximize the expected discounted values of their net future returns, which depend on their ownership type \textit{own}_j. We model three ownership types: for-profit (FP), not-for-profit (NFP) and government (Gov). In our model, a hospital’s ownership type is fixed and cannot be changed.

For a FP hospital, returns are synonymous with profits, while for NFP and government hospitals, returns are a weighted sum of profits, expected patient volume and the provision of service, which we denote as having a positive number of beds.

Specifically, let \textit{beds}_jt denote the number of beds, \textit{EΠ}_jt expected profits net of investment expenses and \textit{EVol}_jt expected volume, all for hospital \textit{j} at time \textit{t}. Then, at any time \textit{τ}, FP hospitals seek to maximize

\[
E_\tau \left[ \sum_{t=\tau}^{\infty} \beta^{t-\tau} \text{EΠ}_jt \right],
\]

while NFPs seek to maximize

\[
E_\tau \left[ \sum_{t=\tau}^{\infty} \beta^{t-\tau} (\text{EΠ}_jt + \alpha^{\text{NFP}}_v \text{EVol}_jt + \alpha^{\text{NFP}}_p \{\text{beds}_jt > 0\}) \right],
\]

(1)

where \(\alpha^{\text{NFP}}_v\) and \(\alpha^{\text{NFP}}_p\) are parameters to estimate.

Note that a weight term on expected net profits for NFPs is not identified: if we included such a term in (1), we could then multiply the three \(\alpha\) terms by a constant and all observable predictions of the model would be the same, as this would effectively just change the units of NFP utility. Hence, in (1), we normalize the weight on expected net profits to be one. We assume that government hospitals maximize a similar objective function to (1), but with weights \(\alpha^{\text{Gov}}_v\) and \(\alpha^{\text{Gov}}_p\).
4.2 Investment in beds and CAH status

We now detail the specifics of the investment processes that determine changes in the number of beds and in CAH status and through this in industry structure. Let $CAH_{jt}$ denote CAH status for hospital $j$ at time $t$. At the start of each period $t$, each hospital $j$ faces a mean cost of investment that is common across hospitals and an $i.i.d.$ shock to its investment cost, $\epsilon_{jt}$. We assume that hospital $j$ knows the value of $\epsilon_{jt}$ prior to making its time $t$ investment decision but that it does not know the value of other firms’ shocks, and we let $\epsilon_{jt}$ be distributed $N(0, \sigma^2)$, where $\sigma$ is a parameter that we estimate.

Knowing $\epsilon_{jt}$, each hospital simultaneously chooses a level of investment $x$ which denotes the number of beds to be added. We allow $x$ to be positive, negative or zero. The investment in beds is realized at the start of the following period. We use the following functional form for investment:

$$
InvCost(x, \epsilon) = 1\{x > 0\}\delta_1 + 1\{x > 0\}\delta_2 x + 1\{x > 0\}\delta_3 x^2 \\
+ 1\{x < 0\}\delta_4 + 1\{x < 0\}\delta_5 x + 1\{x < 0\}\delta_6 x^2 \\
+ 1\{x > 0\}x\sigma_1 \epsilon + 1\{x < 0\}x\sigma_2 \epsilon.
$$

(2)

Our investment choice is motivated by several important factors. In our data, hospitals do not alter their investment level for the vast majority of years. This suggests that there are substantial fixed costs for investment. In addition, the marginal costs of positive investment are likely to be very different than the marginal costs of negative investment. A positive investment involves building a new physical facility and providing medical equipment for that facility. Given the specificity of this investment, the scrap value of selling that facility is likely less than the cost of building it. Thus, we use a quadratic adjustment cost of investment with the cost of investment allowed to be different for positive or negative changes in the number of beds. This specification is similar to that of Ryan (2007) and a long literature that he cites.

Our investment process deviates from the literature in that we allow for the $i.i.d.$ investment cost shock $\epsilon_{jt}$. The use of an investment cost shock allows us to have a model where investment levels can vary for a hospital at a given state, as we find in the data. We let the
effect of this shock vary for a positive or negative investment level, through the parameters $\sigma_1$ and $\sigma_2$, both of which are restricted to be positive. Note that variations in $\epsilon$ will generate variations in investment levels for any state. In particular, a higher value of $\epsilon$ means a higher increment in cost for higher $x$. This implies that investment is weakly decreasing in $\epsilon$ for any state for reasonable profit functions. We impose this weak monotonicity property as an assumption. As we discuss in Section 5 below, the monotonicity assumption allows us to estimate our model with an adaptation of the techniques of Bajari et al. (2007).

A hospital can exit the industry by disinvesting in beds until it has none left. Once a hospital has no beds it is assume to have permanently exited the industry. It can no longer build beds or otherwise earn profits. Like other investment realizations, exits occurs at the start of the following period.

Concurrently with the investment decision, each non-CAH hospital simultaneously decides whether it wants to convert to CAH status. The hospital pays a fee $c^{CAH} \geq 0$ in order to attempt to convert to CAH status in the following period. Conversions to CAH status must be approved by the government and this approval process is lengthy, potentially costly, and uncertain. Hence, we model the CAH approval process as stochastic, with the outcome occurring at the start of the next period. We assume that firms can choose the CAH fee, and that a greater fee results in a greater chance of successful approval of CAH status. Specifically, we let

$$Pr(\text{CAH approval}|c^{CAH}) = 2\exp(\gamma c^{CAH})/(1 + \exp(\gamma c^{CAH})) - 1,$$

where $\gamma$ is a parameter to estimate. Note that the specification is designed to be similar to a logistic model but different in that a firm that pays $c^{CAH}$ of 0 has a zero probability of becoming a CAH hospital.

In our model, CAH hospitals are not allowed to revert to non-CAH status. We define $Pr(\text{CAH approval}) = 0$ for CAH hospitals. Also, we assume that any CAH hospital with more than 25 beds has any beds over 25 removed. We assume that the cost of this elimination of beds is zero. We make this assumption to be consistent with the regulations that specify that CAH hospitals are not allowed to have more than 25 beds.
4.3 Hospital production process

After investment, the hospital production process occurs. Hospitals incur both fixed costs, $FC_{jt}$ and marginal costs $mc_{ijt}$ from treating patient $i$. These costs are known at the start of the third stage. We assume that fixed costs consist of an aggregate term and a hospital-specific term,

$$FC_{jt} = FC + FC_j.$$

Similarly, we assume that marginal costs consist of a patient specific term and a hospital efficiency term,

$$mc_{ijt} = sev_i + \hat{mc}_j.$$

We let $sev_i$ denote the patient’s severity of illness, and allow marginal costs to vary based on severity of illness. Severity of illness, in turn, is a function of DRGs and other observable characteristics.

Patients are also differentiated by their insurance $ins_{it}$ which can be Medicare (Med) or non-Medicare (NM). Knowing their cost structure, hospitals simultaneously set the base price for non-Medicare patients, which we call $p_{jt}$. The price $p_{jt}$ is adjusted based on patient severity of illness, so that the total bill for a patient with base severity $sev_i$ is $p_{jt}sev_i$. Patients, in combination with their insurance companies, will pay the hospital this price upon treatment.

CAH hospitals submit a bill to Medicare for their cost of treating Medicare patients that is based on average cost, which we denote $ac_{ijt}$. Note that

$$ac_{ijt} = \frac{FC_{jt} + \sum_{i=1}^{I} mc_{ijt}}{I}.$$

Medicare reimburses the hospital as a fixed percentage, $r_{CAH}$, of average costs. In contrast, non-CAH hospitals submit $sev_i$ (essentially DRGs) to Medicare, and are reimbursed some fixed percentage $r^M$ of $sev_i$.

Let $Pr_{ijt}$ denote the probability that patient $i$ chooses hospital $j$. Then, we can express expected hospital profits $E\Pi_{jt}$ for CAH hospitals as:

$$E\Pi_{jt}^{CAH} = \sum_{ins_i=Med} Pr_{ijt}r_{CAH}ac_{ijt} + \sum_{ins_i=NM} Pr_{ijt}(p_{jt} - \hat{mc}_j)sev_i - FC_{jt},$$ (4)
while for non-CAH hospitals, the term in the first sum of the equation analogous to (4) would be \( P_{ijt}^{M,sev_i} \).

The final stage is for patients to choose the hospital at which to seek treatment. Each patient makes a discrete choice of one of the hospitals in the market, where the set includes the large, urban hospitals whose decisions we treat as exogenous. An important determinant of hospital choice is distance. Let \( location \) denote geographic location (of a hospital or patient), \( distance_{ij} \) denote the straight-line geographic distance between patient \( i \) and hospital \( j \), \( closest_{ijt} \) be a dummy for the hospital being the closest to the patient at time \( t \) and \( teach_j \) is a dummy taking the value of one if the hospital is a teaching institution.\(^9\)

Let us first consider Medicare patients. These patients pay only a fixed deductible for the hospital treatment. Since we assume that patients are constrained to choose some hospital, we can ignore this deductible. We can write the utility function for Medicare patients as

\[
\bar{u}_{ijt}^{Med} = h^{Med}(dist_{ij}, closest_{ij}, beds_j, CAH_j, teach_j) + e_{ijt},
\]

where \( e_{ijt} \) is a type I extreme value residual. Note that our model of patient utility allows for the fact that patients with a high severity of illness may prefer bigger hospitals, and allows for CAH status to directly influence the utility of patients.

Let us now consider non-Medicare patients. Non-Medicare patients will pay a coinsurance, which amounts to a fixed percentage of the cost of their care, \( copay \). Thus, the price faced by non-Medicare patient \( i \) is \( copay \cdot p_{jt} \). The utility function for non-Medicare patients is identical to (5) except for the addition of a new argument, \( copay \) and \( p_{jt} \) to their expected utility \( h^{NM}(dist_{ij}, closest_{ij}, beds_j, CAH_j, teach_j, p_{jt}) \).

Given the type I extreme value error assumption, we can use (??) to write the choice probability for Medicare patients as

\[
P_{ijt} = \frac{\exp(\bar{u}_{ijt}^{Med})}{1 + \exp(\bar{u}_{ijt}^{Med})}
\]

with an analogous expression for non-Medicare patients. Similarly, the expected volume for

\(^9\)A teaching hospital is defined as having at least .25 residents per bed
the hospital can be expressed as

\[ EV_{ol_{jt}} = \sum_{i=1}^{I} P_{rijt}. \]  

(6)

### 4.4 Firm optimization and equilibrium

Using the industry structure and preferences that we have described above, we can define the optimization problem for the firm and use this to characterize the Markov Perfect equilibrium of the industry. We start by defining the state space as the set of payoff relevant state variables, consistent with the definition of Markov Perfect equilibrium.

The state for a given hospital consists of its characteristics and the characteristics of the expected consumers and firms near it. We can group a hospital’s characteristics together as \(hospchar_{jt} = (\text{beds}_{jt}, CAH_{jt}, \hat{mc}_{j}, FC_{j}, own_{j}, location_{j})\) and the characteristics for a patient together as \(patchar_{i} = (\text{sev}_{i}, ins_{i}, location_{i})\). We further group together the aggregate industry state at time \(t\) as \(\Omega_{t} = (hospchar_{1t}, \ldots, hospchar_{jt}, patchar_{1}, \ldots, patchar_{I})\). Hospital \(j\)’s state can then be described as the industry state and the hospital’s position within this state, \((\Omega_{t}, j)\).

Using this definition of the state space, we can write the single-agent decision problem for the firm and use this to exposit the properties that must hold in a Markov Perfect equilibrium. We start by analyzing the per-period return. At any period, a firm will earn a return that is a function of its state, action \((x, c^{CAH})\) and unobservable \(\epsilon\). Let this function be denoted \(TR((x, c^{CAH}), (\Omega_{t}, j), \epsilon)\). We can write this vector as:

\[
TR((x, c^{CAH}), (\Omega_{t}, j), \epsilon) = E\Pi(\Omega_{t}, j) + \alpha_{p}^{Gov} - InvCost(x, \epsilon) - c^{CAH} \\
+ 1\{own_{j} = NFP\} \left(\alpha_{v}^{NFP} EV_{ol_{jt}} + \alpha_{p}^{NFP} \cdot 1\{\text{beds}_{jt} > 0\}\right) \\
+ 1\{own_{j} = Gov\} \left(\alpha_{v}^{Gov} EV_{ol_{jt}} + \alpha_{p}^{Gov} \cdot 1\{\text{beds}_{jt} > 0\}\right).
\]

(7)

Note that \(TR\) is different than just net profit maximization because NFPs and government hospitals maximize a weighted sum, not just profits.

Using (7), we can define the net expected total returns to firm \(j\) at the start of any period...
t as \( V(\Omega_t, j) \) and express \( V(\Omega_t, j) \) recursively as the following Bellman equation:

\[
V(\Omega_t, j) = \int \max_{x, c^{CAH}} \{ TR((x, c^{CAH}), (\Omega_t, j), \epsilon) + 1\{beds_{jt} + x > 0\} \beta E [V(\Omega_{t+1}, j) | (\Omega_t, j), (x, c^{CAH})] \} dP(\epsilon),
\]

where the law of motion for the \( j \)th component of \( \Omega_t \), is

\[
beds_{j,t+1} = beds_{jt} + x \quad \text{and} \quad CAH_{j,t+1} = CAH_{jt} + Pr(\text{CAH approval}|c^{CAH}).
\]

The Bellman equation (8) reflects the fact that if firm \( j \) exits, it receives no further returns. If firm \( j \) does not exit, then its returns depend on the law of motion for the non-\( j \) components. Firm \( j \) takes these as given and never as a function of \( x \) or \( c^{CAH} \). Standard arguments show that the Bellman equation (8) has a unique fixed point provided that \( \beta < 1 \) and profits are bounded.

Using the definition of the Bellman equation, we can now define a Markov Perfect equilibrium. The Markov Perfect equilibrium is a set of investment strategies for every state and shock, \( \hat{x}(\Omega_t, j, \epsilon) \) and \( \hat{c}^{CAH}(\Omega_t, j, \epsilon) \), for which the following property holds: for each firm \( j \), \( \hat{x} \) and \( \hat{c}^{CAH} \) satisfy the Bellman equation (8) given that the law of motion for other firms is derived from \( \hat{x} \) and \( \hat{c}^{CAH} \) applied to an analogous equation to (9). This condition ensures that no unilateral deviation is profitable at any state.

5 Inference

5.1 Overview of method

The structural parameters of our model are the \( \alpha \) objective function parameters, the \( \delta \) investment cost parameters, the discount factor \( \beta \), the CAH conversion cost parameter \( \gamma \), the static marginal cost and fixed cost parameters, and the \( \tau \) consumer utility parameters. We deal with these parameters with a variety of methods. We estimate the consumer utility parameters \( \tau \) using a standard multinomial logit maximum likelihood model, as the consumer
does not face a dynamic problem. We observe profits in the data and hence we directly estimate profits, rather than estimating costs and demand and inferring profits from these, as is typically done. It is difficult to identify the discount factor and hence we set it to $\beta = .95$.

The remaining parameters, $\alpha_p^{NFP}, \alpha_v^{NFP}, \alpha_p^{Gov}, \alpha_v^{Gov}, \delta_1, \ldots, \delta_6, \sigma_1, \sigma_2$ and $\gamma$ are not directly observable in the data but can, in principle, be identified by firm behavior. Since firm behavior is a function of the dynamic oligopoly model evaluated at the Markov Perfect equilibrium, identification of these parameters generally requires imposing the structural model.

A method for estimating the structural parameters of dynamic models was developed by Rust (1987) and applied to the dynamic oligopoly setting by Gowrisankaran and Town (1997). The idea of these methods is to perform a non-linear search for the structural parameters that best fit the data. For any vector of structural parameters, one solves for the Markov Perfect equilibrium of the industry and then evaluates “fit” as the closeness of the actions predicted by the equilibrium of the model to those reported in the data. The problem with these methods is that they are extremely computationally intensive as they require solving the Markov Perfect equilibrium repeatedly, which is very time-consuming.

More recent methods to estimate dynamic models are based on the idea that one can use the data themselves to predict the future actions of the firm and its competitors, rather than solving for the Markov Perfect equilibrium for each parameter vector, since the data reflect Markov Perfect equilibrium play. To implement these methods, one generally predicts future decisions with a non-structural first stage. The second stage then involves a non-linear search over structural parameters where the econometrician has only to solve for the optimal current decision of the agent taking the future actions as given.

We base our estimation algorithm for these remaining parameters on one variant of these methods, that developed by Bajari et al. (2007). The BBL method has two useful features for our purposes. First, rather than solving for the overall optimal decisions (as above) they show that one can estimate the structural parameters by finding the policies that are optimal within a finite set of alternate policies. This is particularly useful for models with continuous action spaces as otherwise, solving for optimal decisions is computationally difficult. Second,
they show that the second stage can be evaluated with a very quick computational process, which is similar to non-linear least squares, provided that one can express the expectation of the total return for any state, action and unobservable, $TR((x, c^{CAH}, (Ω_t, j), ε)$ as a linear combination of the structural parameters and functions of the data, which we can.

Following BBL, we develop the linear representation for our model, by writing

$$E \left[ TR((x, c^{CAH}, (Ω_t, j), ε) \right] = Ψ((x, c^{CAH}, (Ω_t, j), ε) \cdot θ,$$  \hfill (10)

where $Ψ$ is a vector-valued function of the data, $θ$ are the structural parameters, and the (linear) dot product of these two terms generates expected total returns. We use (10) to exposit the value function similarly as:

$$V(Ω_t, j) = E_t \left[ \sum_{τ=t}^{∞} β^{τ-t} Ψ((\hat{x}(Ω_t, j, ε), C^{CAH}(Ω_t, j, ε)), (Ω_t, j), ε) \right] \cdot θ,$$  \hfill (11)

where the expectation is over current and future unobservables and future states given unobservables and equilibrium actions. Define $W(Ω_t, j)$ to be the expectation term in (11).

Using these definitions, which are analogous to BBL, we adapt the BBL methods to our model and data with the following algorithm. First, we approximate the law of motion for the industry as a function of states and actions, and static gross profits and actions as a function of states. Second, we forward simulate the industry given equilibrium actions to approximate $W(Ω_t, j)$ for every state observed in the data. Third, we choose a set of counterfactual investment policies. Let there be $P$ such policies in the set. By the Markov Perfect equilibrium assumption, each such policy must yield a weakly lower expected value when chosen by a firm faced by firms playing the Markov Perfect equilibrium strategies. Thus, for each counterfactual policy, we forward simulate to evaluate an analog to $W(Ω_t, j)$ where the state transitions are determined by the counterfactual policy. Let $\hat{W}^p(Ω_t, j)$ denote one such vector. Fourth, using (11), the calculated $W(Ω_t, j)$ and the set of $\hat{W}^p(Ω_t, j)$, we estimate the vector of structural parameters as the values for which the true policies are most closely optimal.

Recall that in our model, the unobservable investment shock $ε$ will affect the choice of investment at any state. The models given in Bajari et al. (2007) and Ryan (2006) do not
allow for private information shocks to investment or other choice variables that affect the state. In estimating (10), one must take into account the correlation between the investment level and ε in order to accurately recover the cost of investment. To see this, note that in our model, the investment policy  \( \hat{x}(\Omega_t, j, \epsilon) \) is weakly declining in \( \epsilon \) for any given state, or alternately put, firms with a low cost of investment invest more at any state. If one instead assumed that the distributions of investment and cost shocks were uncorrelated, one would overstate the costs of investment. The difficulty is that we do not directly observe the cost shock for any investment level, and hence cannot directly compute \( \Psi((x, \epsilon^{CAH}), (\Omega_t, j), \epsilon) \).

We develop a method that allows us to account for this endogeneity of investment in a way that preserves the linearity of the estimation specification in (10). Our method rests on a simple consequence of the monotonicity of investment: a firm that invests in the \( x \)th percentile of the investment distribution must have obtained a draw of \( \epsilon \) that is in the \( 1 - x \)th percentile of the \( \epsilon \) distribution. Let \( F_{\Omega_t,j}(x) \) denote the inverse c.d.f. for investment at state \((\Omega_t, j)\). Then, for any observed investment level \( x > 0 \), in equilibrium,

\[
\epsilon_{j,t} = \sigma_1 \Phi^{-1}(1 - F_{\Omega_t,j}(x)),
\]

where \( \Phi^{-1} \) is the inverse of the standard normal c.d.f. Since the only component of (12) that is unobservable is \( \sigma \) and \( \sigma \) enters linearly in (12), we can construct terms in \( \Psi \) that account for this correlation, as we do below.

A potential problem to this approach is the fact that investment is only weakly monotonic in \( \epsilon \): because of the fixed costs of investment, there will be a discrete mass of \( \epsilon \) for which investment is 0. However, the lack of strict monotonicity is not problematic, since the only mass point is at investment of 0, and the value of \( \epsilon \) does not affect costs when investment is 0.

Another issue is how to estimate the costs of CAH conversion. Note that the CAH conversion strategy is a function, effectively of state variables and investment. Let \( P^{CAH}(\Omega_t, j, x) \) denote the probability of CAH conversion for any state and investment level. Then, from (3),

\[
\gamma^{CAH} = \log \left( \frac{1 + P^{CAH}(\Omega_t, j, x)}{1 - P^{CAH}(\Omega_t, j, x)} \right).
\]

20
Noting that the right side of (13) can be approximated by the data, as in (12), one can again construct a term in $\Psi$ that accounts for the cost of conversion, $c^{CAH}$. One can redefine $\Psi$ to have it be a function of $P^{CAH}$ rather than $c^{CAH}$, as $P^{CAH}$ is really what is observed in the data.

Using these formulations, our vector $\Psi$ has the following components:

$$\Psi((x, P^{CAH}), (\Omega_t, j), \epsilon) = (\Pi(\Omega_t, j),$$

$$1\{\text{own}_j = NFP\}EVol(\Omega_t, j), 1\{\text{own}_j = NFP\}1\{\text{beds}_{jt} > 0\},$$

$$1\{\text{own}_j = Gov\}EVol(\Omega_t, j), 1\{\text{own}_j = Gov\}1\{\text{beds}_{jt} > 0\},$$

$$-1\{x > 0\}, -1\{x > 0\}x, -1\{x > 0\}x^2, -1\{x < 0\}, -1\{x < 0\}x,$$

$$-1\{x < 0\}x^2, -1\{x > 0\}x\Phi^{-1}(1 - F_{\Omega_t,j}(x)), -1\{x < 0\}x\Phi^{-1}(1 - F_{\Omega_t,j}(x)),$$

$$- \log[(1 + P^{CAH}(\Omega_t, j, x))/(1 - P^{CAH}(\Omega_t, j, x))].$$

The corresponding vector $\theta$ is:

$$\theta = (1, \alpha^{NFP}_v, \alpha^{NFP}_p, \alpha^{Gov}_v, \alpha^{Gov}_p, \delta_1, \delta_2, \delta_3, \delta_4, \delta_5, \delta_6, \sigma_1, \sigma_2, 1/\gamma).$$

It is easy to verify that the resulting dot product is equal to $TR((x, c^{CAH}), (\Omega_t, j), \epsilon)$.

Using the approximations for $W$ and $\hat{W}^p$, we use the same one-sided non-linear least squares approach as in BBL. Specifically, we choose our parameter estimates to minimize:

$$\sum_{p=1}^{P} \sum_{t,j \in \text{sample}} 1\{\hat{W}^p(\Omega_t, j) \cdot \theta > W(\Omega_t, j) \cdot \theta\}(\hat{W}^p(\Omega_t, j) \cdot \theta - W(\Omega_t, j) \cdot \theta)^2.$$

We obtain standard errors for the coefficients by bootstrapping the above four-step process.

### 5.2 Estimation of dynamic firm parameters

Our estimation algorithm depends on many necessary specifications and approximations that we list here. Most importantly, the state space of this problem, $(\Omega_t, j)$, is too large for computational purposes, as it includes the characteristics of all hospitals and patients in the market. Thus, we approximate the state space by summarizing it in relatively few dimensions. The important attributes that define the state for a hospital include its characteristics, some
weighted sum of the characteristics of its competitors based on how close competitors they are, the level of competition, and the size of the market surrounding it.

For a given hospital, three of the characteristics noted in $hospchar_{jt}$ enter directly: $CAH_{jt}$, $beds_{jt}$ and $own_{jt}$. The final characteristics are fixed and marginal costs. We estimate a hospital-specific productivity level, $\hat{\text{cost}}_{jt}$ to capture the fixed and marginal costs of a hospital. We estimate this value for each hospital as the hospital fixed effect from a regression of profits on characteristics, using data from before the start of our sample, from 1995 to 1997.\footnote{Our use of this type of parameter is similar to Dunne et al. (2008).} Because $\hat{\text{cost}}_{jt}$ must capture variations in both fixed and marginal costs, we put in polynomial terms and interactions of it with other state variables in the regression of profits on states.

We also need to summarize the characteristics of patients and other hospitals in the surrounding market for any hospital. We measure these with three state variables for any hospital: summary measures of the number of Medicare and non-Medicare patients who are likely to be treated at any hospital, a measure of competition and the weighted CAH status of other hospitals. These terms together capture the size of the market and the degree of competitiveness of the market. We calculate the expected number of patients by estimating the Medicare utility function (5).\footnote{For non-Medicare patients, we also use this function which is equivalent to assuming that the prices faced by these patients are the same across hospitals.} We then use these to calculate expected volume by insurance type, $EVol_{jt}^{Med}$ and $EVol_{jt}^{Non-Med}(\Omega_j, t)$, analogously to $EVol_{jt}$ in (6).

In order to measure the level of competition in the market, we could potentially use a variety of measures related to the number of other hospitals nearby. A Herfindahl index is a convenient summary statistic from among these. Rather than arbitrarily defining a market over which to calculate a Herfindahl index, we follow the literature on the hospital industry (e.g., Kessler and McClellan, 2000) and define a patient-weighted Herfindahl index. Specifically, we start by defining

$$H_{it} = \sum_j P_{it}^{2}_{ijt}. \tag{7}$$

We then weight the Herfindahl index for each patient by the probability that they choose a
given hospital. This gives us the measure that we use in our state space, the patient-weighted Herfindahl index:
\[
HHI_{jt} = \frac{\sum_i P_{r_{ijt}} H_{it}}{EV_{ol_{jt}}},
\]
which provides a summary statistic for the level of competition faced by each hospital.

Similarly, we define the CAH status of a hospital’s competitors, \(CAH_{comp_{jt}}\) as the patient-weighted sum of the CAH status of competitor hospitals. For each patient, the CAH status of competitor hospitals is defined by the weighted sum of the CAH status for competitor hospitals to \(j\), weighted by the probability that the patient seeks care at any of these hospitals. Thus,
\[
CAH_{comp_{jt}} = \left( \sum_i P_{r_{ijt}} \frac{\sum_{k \neq j} P_{r_{ikt}} CAH_{kt}}{\sum_{k \neq j} P_{ikt}} \right) / EV_{ol_{jt}}. \tag{15}
\]
Combining all these variables, the state space that we use in the analysis is \(\Omega = (\text{beds}, CAH, \hat{\text{cost}}, own, EV_{ol_{Med}}, EV_{ol^{Non-Med}}, HHI, CAH_{comp})\).

We now discuss how we solve for the first-stage static profit functions and actions and the low of motion at each state. Ideally, we would solve non-parametrically for these functions. However, this is not possible because of the large dimensionality of the problem. Since the state space is continuous, we solve for these functions with regressions. Specifically, group together the state vector and interactions and polynomials of the states as \(r(\Omega)\). Then, we perform a linear regression of profits on \(r(\Omega)\), where the exact specification is given in the results section.

In our model, CAH status is an absorbing state. Thus, we require an estimate of the hazard for \(P^{CAH}(\Omega_t, j, x)\), the probability of successful conversion to CAH between time \(t\) and time \(t+1\) at any state for which \(CAH = 0\). We specify this hazard as a logit, and estimate it via maximum likelihood for non-CAH hospitals, of CAH approval on interactions of \(r(\Omega)\) and investment, which we denote \(\hat{r}(\Omega, x)\). Note that, given our model, it is appropriate to include investment as a regressor in this specification, unlike for the profit regression.

The specification for investment, \(x_{jt}(\Omega)\), is more complicated to design. The majority of years, hospitals do not change their number of beds, or equivalently, they invest nothing. It is important to capture this feature of the data, because the fixed costs of investment will
be identified by the extent to which firms choose to invest in lumpy amounts. Yet, a linear regression cannot model this type of mass-point. This suggests a latent variable model with a mass-point at zero. We estimate the following specification:

\[ x_{jt}^*(\Omega) = r(\Omega)b + e_{jt}, \]

where:

\[ x_{jt} = x_{jt}^* \text{ if } x_{jt}^* < 0, \]
\[ x_{jt} = 0 \text{ if } 0 \leq x_{jt}^* < \bar{x}, \]
\[ x_{jt} = x_{jt}^* - \bar{x} \text{ if } x_{jt}^* \geq \bar{x}, \]
\[ e_{jt} \sim N(0, \sigma_x^2). \]

We estimate the parameters of (16), \( b, \bar{x} \) and \( \sigma_x^2 \), using maximum likelihood. Note that our specification is similar to a Tobit model, but different in that the mass-point is in the middle, not on one end.

The state vector also contains four other variables that evolve over time as a function of the strategies of a hospital and its competitors. We estimate the transition for three of them, \( EVol^{Med}, EVol^{Non-Med} \), and \( HHI \) as linear regressions where the difference between the value at time \( t+1 \) and \( t \) is regressed on \( \hat{r}(\Omega, x) \) for time \( t \). For \( CAH_{comp,jt} \), investment does not enter since it is not a function of firm \( j \)'s decision. Thus, we specify the transition for this variable to include only \( r(\Omega) \).

Using these specifications, we implement the second-stage forward simulation process to compute \( W \) and \( W_p \). We perform this process as follows, for each state. We first draw a value for \( \epsilon \) and use this value to evaluate the simulated investment level. We then use \( r(\Omega) \) or \( \hat{r}(\Omega, x) \) (as appropriate) to simulate the CAH probability and the other laws of motion. If the value of any of these variables falls below 0 we set it to 0. Similarly, if the value of \( HHI \) of \( CAH_{comp} \) rises above 1 we set it to 1.

This process requires simulating unobservables for each of the equations. To simulate CAH approval, we estimate the approval probability for each state and then simulate with this probability. We simulate from the regressions for the linear transitions non-parametrically: we recover the distribution of the fitted residuals from the transition regressions and draw from this distribution. We cannot simulate non-parametrically for investment, since we do
not observe the exact residual when investment is 0, which occurs when $x^*_jt \in [0, \bar{x})$. For values in this interval, we use the estimated normal density, while we estimate the residuals non-parametrically for values outside this interval.

5.3 Estimation of patient utility parameters

We estimate the parameters of the indirect utility function characterized in (5) for Medicare and non-Medicare patients using a maximum likelihood procedure. Specifically, we use the California OSHPD data on a subsample of California patients. For each patient we match latitude and longitude information to their reported home ZIP code and calculate straight-line distances to each hospital in their choice set. We limit the choice set to all hospitals within 150km circle of the patient’s ZIP code. We also allow for the possibility of an outside good which is admittance to a hospital outside of the 150km circle.

The estimates from the patient flow model do not directly enter into the estimation. Rather, we use the estimated parameters from (5) together with locations of patients and hospitals to calculate the characteristics of the hospital’s state space, specifically $EVol^{Med}_jt$, $EVol^{Non-Med}_jt$, $HHI_{jt}$, and $CAH_{Comp_{jt}}$. To perform this calculation, we need locations nationally and not just for California. Thus, we use Census data as our patient sample for this prediction. For each person in the relevant patient category we draw a 150km circle about the tract and calculate $Pr_{ijt}$ for each person in that tract. Once this calculation is made it is straightforward to calculate all of the state space variables for all hospitals in our sample.

5.4 Identification

Although we have specified a relatively intricate dynamic model of interaction between hospitals, the forces that will identify the parameters of interest are reasonably straightforward. The $\tau$ consumer utility parameters will be identified from the extent to which consumers choose hospitals based on characteristics such as location, severity of illness and hospital size.
The parameters in $\theta$ are identified by revealed preferences applied to our dynamic oligopoly model. Specifically, optimal behavior implies balancing the costs of investment, CAH conversion costs and fixed costs against the benefits in the form of profits and other returns. Different values of $\theta$ will imply different trade-offs, and the data will reflect particular trade-offs and hence particular values of $\theta$. Since we use the accounting data on profits in our estimation, much of the identification derives from the shape of the gross profit function and the pattern of exit with respect to different states.

In particular, the bed investment cost parameters $\delta$ are identified by the impact of changing beds on the profit function. Heuristically, optimal investment levels will be higher if gross profits are more steeply sloped in beds, all else being equal. Since investment levels and the shape of profits with respect to beds are observed in the data, the relation between investment and the slope of profits in beds will identify the value of the investment cost parameters. The $\gamma$ parameter on the cost of CAH conversion is similarly identified by the extent to which hospitals obtain CAH status at states where it is profitable to have achieved that status. For instance, if hospitals rarely achieve CAH status even when profitable, this suggests that a small $\gamma$ is making the CAH conversion process very costly.

These arguments are heuristic rather than formally true because of the dynamic oligopoly that is built into our model: an investment in beds will not just change beds, but will potentially change the expected future value of all the state variables, through the interactions that occur between firms. For instance, an increase in beds may cause other firms to reduce their beds in expectation, in which case this positive strategic effect would need to be added to the direct effect of beds on profits. Moreover, firms must jointly decide on the decisions for investment in beds and CAH status. Nonetheless, a simple heuristic benchmark estimate for our investment parameters can be derived by evaluating the average impact of beds on profits, where profits are weighted by $1 - \beta$, and estimating the optimal level of investment given this simple model.

Note that there are seven different $\delta$ parameters. The first six of these parameters relate to the different mean fixed and marginal costs of positive and negative investment. These parameters can all be separately identified by the relative extents of strictly positive and
negative investments in beds and the extent of non-zero investment. In particular, the fact that most periods firms rarely invest suggests a large positive fixed cost of investment.

The two other parameters in the bed investment equation (2), $\delta_7$ and $\sigma$ relate to the distribution of investment for any state. The larger the variance of investment outcomes for a given state, the larger will be $\sigma$. Here, we estimate a distribution with two parameters, essentially two halves of two normal densities that intersect at 0. The $\delta_7$ parameter is then identified by the relative variance of outcomes for negative investment to positive investment.

The final parameters that we estimate via the dynamic model relate to the objective functions by ownership type. These parameters can be identified by the pattern of exit in the market and the relation of exit to profits. For instance, if NFPs often do not exit even when the expected future profit path is negative, this suggests that they value the provision of service and/or patient volume. If it further turns out that in unprofitable markets, NFP hospitals remain in operation only when their expected volume is high, this suggests that NFPs value expected volume rather than simply the provision of service. Again, expected profits and expected volume are a function of the dynamic oligopoly behavior between firms. Yet, one can heuristically benchmark these parameters by examining the exit behavior by types as a function of current profits.

6 Results

6.1 Evidence on the Impact of the CAH Program

We present some evidence of the impact of the CAH program on the rural hospital performance and market structure. First, summary statistics of our sample of small rural hospitals at risk for CAH conversion are presented in Table 3. Our sample is 51% NFP. Local government hospitals comprise 39% of the sample and 11% of the sample are for-profit hospitals. The typical hospital faces some measured competition with an $HHI$ is .42. Over the sample period the rural hospitals on average reduced their beds by 1.78. The closure rate is .008.

Table 4 compares CAH and non-CAH hospitals in the same sample for 2005. The table
shows that CAHs are substantially smaller than non-CAH hospitals, which is to be expected given the regulatory framework they face. The average number of beds for CAHs is 22.47, very close to the upper bound of 25 beds. In Figures 3 to 4 we present the histograms of bed size for rural hospitals for 1996 and 2005. From this picture it is clear that the CAH program had large effects on the size distribution of rural hospitals. Figures 5 and 6 present the bed size histograms for hospitals that ultimately converted to CAH status in 1996 and in 2005. Not surprisingly, CAH conversion dramatically altered the distribution of the number of beds per hospital. Furthermore, the large mass point at 25 beds suggests that the 25 bed limit is a binding constraint, i.e. CAHs would increase their bed size if the regulations allowed it.

With respect to ownership of CAHs, there is very little participation of for-profit organizations (4%), and large participation of government-owned hospitals (46%). In markets where CAHs are present, the percentage of Medicare-eligible residents averages 16% (shown in Table 4) and it is statistically significantly bigger ($t=11.22$) than the percentage of Medicare eligibles in areas where non-CAHs are present. This suggests that hospitals are responding to the incentives of the program, which is available only for Medicare reimbursement. In Figure 7 we present the time series of accounting profit (net income) margins, $\frac{\text{Profits}}{\text{Total Revenue}}$, for hospitals with less than 225 beds in 1995 by rural status. The time series pattern for profit margins is striking. Prior to the passage of the BBA which initiated the CAH program, profit margins in rural and non-rural hospitals were very similar. With the passage of the BBA, hospital in non-rural areas saw a dramatic decline in margins as the BBA dramatically cut Medicare payments to non-CAH hospitals. However, hospitals in rural areas saw little decline in their profit margins following the passage of the BBA. This simple graph is consistent with the findings of MedPAC (2005) and Stensland et al. (2003) where they found that hospitals that converted to CAH increased their margins significantly more than a sample of non-converting hospitals. Figure 8 shows that the exit rates of urban and rural hospitals move together during the period we study, and the difference in exit rates between rural and urban hospitals is amplified after the passing of the legislation.

12 The rise of HMOs, which did not significantly impact rural areas, peaked around 1997 and may also explain some of the decline in profit margins for non-rural hospitals in the late 1990s.
6.2 First Stage Estimates

In the first stage we recover the parameters from patients’ demand, hospitals’ profits, and the policy functions for CAH conversion, investment and exit. The goal is to characterize accurately the behavior of the hospitals at every state, which is necessary for the second stage estimation of the dynamic parameters. Consumers’ preferences for hospitals were estimated by means of a multinomial logit model, where hospitals were represented as a bundle of attributes including distance from the patient’s census tract, whether the hospital is the closest to the patient, capacity measured by beds, CAH status, and teaching status. We estimate the preferences for both Medicare and private patients using discharge data from the California OSHPD. The probabilities generated by this model are the ones used to compute the expected volumes described in the model section of the paper. The estimates of the preference parameters are presented in Table 5. It can be seen that Medicare patients present a larger disutility from hospital distance relative to the younger population. The preferences for the rest of the attributes are very similar between the two groups.

The results from the regression of profits on states are presented in Table 6. Due to the large number of interactions included in the regression, we summarize the important results in Figure 9. As it is shown in the figure, the benefits from CAH conversion are larger for the hospitals that actually converted than to the non-converters had they converted at every level of productivity. In addition, it can be seen that the low performing hospitals are the ones that benefit the most from conversion. For a hospital with average productivity, conversion to CAH status implies an increase in profits of about $260,000 per year, and almost twice as much for a hospital at the bottom 10th percentile.

Table 7 presents the estimates of the CAH conversion policy function, estimated with a probit model. The probability of converting is larger for NFP and government hospitals relative to for-profit hospitals. Larger hospitals and more productive hospitals are less likely to convert, as are the hospitals that show positive investment in capacity. Table 8 presents the results from our tobit-like regression for investment, where the parameters $b$, $\bar{x}$ and $\sigma_x$

\footnote{Future work will incorporate states that we believe are more representative of the rural population such as Iowa and Washington, and will include pre-policy and post-policy data.}
are estimated. In addition to the policy regressions, we estimate the laws of motion for the state variables $HHI$, $EVol^{Med}$, $EVol^{Non-Med}$, $HHI$ and $CAH_{comp_{it}}$, as linear regressions where the differences between the value at time $t+1$ and $t$ are regressed on polynomials of the state variables. These results are available upon request.

6.3 Dynamic Parameter Estimates

The parameter estimates of the second stage are presented in Table 9. These are the parameters of hospitals’ objective functions, investment cost, and CAH investment that rationalize the policy functions estimated in the previous section. Most parameters are estimated precisely, as evidenced by the bootstrapped standard errors.

The first four parameters indicate that non-profit and government hospitals value being in operation. However, we also find that hospitals prefer having less patient volume, all else being equal. Since profits are measured in thousands of dollars and volume in thousands of Census individuals in the market, our estimates of $\alpha_{v}^{NFP}$ imply that non-profit hospitals are indifferent between making an additional $76$ in profits and having $1$ less patient in their market. If patients have a $1/100$ chance of actual admission, this implies $7600$ additional profits for $1$ less patient served in a year. Thus, although the sign of this coefficient is counterintuitive, the magnitude is small. Our estimate of $\alpha_{p}^{NFP}$ implies a larger coefficient on presence, as presence is worth $2.98$ million to a NFP hospital. Government hospitals value volume and remaining operating similarly to NFPs.

The estimates of the parameters of the investment cost function, $\delta_{1}, \ldots, \delta_{6}$, show that the costs of positive investment are positive, with the cost of one new bed being $3.41$ million. The quadratic term on positive beds is very small, implying that the marginal cost of additional beds is roughly the same as the cost of the first bed. The initial fixed cost of positive bed investment is also small, roughly -$200,000.

We find that disinvestment is also costly with an initial marginal cost of $1.80$ million per bed and an initial fixed cost of $480,000. Moreover, this cost is convex, with the marginal cost at $10$ beds increasing by $41,000$ relative to the initial marginal cost. The convexity and
positive costs of disinvestment are consistent with the fact that hospital beds cannot be sold and reused easily.

The standard deviation of the per-bed costs is also substantial, $1.09 million for positive beds or $1.56 million for negative beds. This is the result of there being substantial variation in observed firm behavior for any given state.

The last parameter in Table 9, $\gamma^{-1}$ is the CAH approval process parameter. If a hospital invests $1,000 in acquiring CAH status, it has a probability of .5% of being approved. If the hospital invests is $150,000, the probability of approval increases to 63.9%. This latter figure of $150,000 corresponds to about one third of the average CAH hospital annual accounting profit.

7 Policy Experiments

In this section we provide the results from a counterfactual experiment that aims at finding the impact of the CAH program. We do this by solving for and simulating the equilibrium under the counterfactual scenario that CAH conversion is not available. In the interest of computational simplicity, we define markets using a narrower definition than for the estimation, 50 km instead of 150 km, and divide the U.S. into mutually exclusive markets based on hospitals which are candidates for conversion. We also allow for patients to choose larger and urban hospitals. These are modeled as exogenous players, which do not adjust their beds in response to decisions from the CAH candidate hospitals.

We solve for the Markov Perfect Equilibrium along the lines of Ericson and Pakes (1995) using the structural parameters estimated above. We use the initial conditions from 2005, the last year of our data, and assume that these conditions persist forever. Our initial policy experiments examine the Western states of WA, OR, CA, AZ, NM and NV. There are 98 such markets. Also, we initially only keep markets for which there are no other CAH candidate hospitals within the 50 km zone. This leaves 67 markets for which the hospital is the only strategic player, although many of these markets have larger or urban hospitals within the 50 km zone.
Our first policy experiment simulates the outcomes of the equilibrium for a baseline and compare them to the counterfactual where conversion to CAH is not an option. Figure 10 shows the exit probabilities for the hospitals that converted, had they not converted to CAH over a 20-year period. In a period of 20 years, about 6% of those hospitals would have exited the market. With the CAH program, the exit rate is zero.

As expected, the program also affected hospitals’ capacity as shown in Figure 11. Mean capacity is roughly 5 beds lower with the CAH policy than without the policy. In Figure 12 we plot the effect of the CAH program on hospitals’ value. We find that the program’s effect on hospital value is largest for very small and very large hospitals. For a 25-bed hospital, the program increases expected discounted value by approximately 30%. The finding on large hospitals is probably due to the small number of large hospitals in our at-risk sample in conjunction with the quadratic specification for profits.

In contrast to the increase in value of hospitals, the mean expected discounted utility for patients is lower with the CAH program. The reason for this is that we estimate patients to have a significant disutility from being treated at a CAH (see Table 5). Yet, for 15 of the 67 markets, consumers benefit from the CAH program. We can also compare expected discounted patient utility to firm value. Adding in the change in government revenue from the CAH program will provide reasonable total welfare numbers from the policy change.

We can also examine other policies, including changing the number of beds for inclusion in CAH program and changing the program to result in a lump-sum transfer to hospitals.

8 Conclusions

In this paper we seek to understand the impact of the CAH program on the rural hospital industry market structure. To evaluate the impact of the program we estimate a dynamic oligopoly game, where hospitals take into account the effect of their decisions on rivals. The estimation is performed using the recent two-step BBL procedure, which we modify by introducing private information in the investment cost function. The CAH program has dramatically transformed the rural hospital landscape. Incentives provided in the program
radically reduced the average bed size of rural hospitals. Furthermore, our initial estimates suggest that the CAH program increased profits for converting hospitals, and disproportionately so for poor performing rural hospitals. That is, insofar as the program’s intent was to provide extra assistance to hospitals that were at risk of failing, it achieved that goal. Our initial estimates are generally sensible and have several interesting implications. Non-profit and government hospitals intrinsically value treating patients and remaining open in addition to profits. Hospitals’ cost of investment is asymmetric for bed investment and disinvestment. Simulations in markets with only one candidate CAH hospital show that the program prevented exit by 6% of hospitals closures had the program not been implemented. Our work contributes to a recent and fast growing literature that uses the results from the estimation of dynamic games to perform policy evaluations. It should be noted that these results are very preliminary and subject to evolution. Future work will include multi-agent simulations and welfare calculations to provide an overall assessment of the program.
References


Figure 1: Conversion rates and Percentage of CAH Hospitals in the U.S.

Figure 2: Spatial distribution of CAH. Dots represent CAH, polygons represent MHAs.
Figure 3: Histogram of bed size, rural hospitals, 1996

Figure 4: Histogram of bed size, rural hospitals, 2005
Figure 5: Histogram of CAH converters, 1996

Figure 6: Histogram of CAH converters, 2005
Figure 7: Mean profit margins for hospitals with less than 225 beds in 1995.

Figure 8: Exit rates for Rural, Urban and All U.S. Hospitals
Figure 9: Change in profit from CAH conversion by CAH status and productivity ($1,000)

Figure 10: Impact of CAH program on exits
Effect of CAH policy on Hospital Size

Figure 11: Impact of CAH program on size distribution

Relative Value with Option to Convert

Figure 12: Impact of CAH program on hospital value by number of beds
<table>
<thead>
<tr>
<th>Legislation</th>
<th>Key Aspects of CAH Legislation and Regulation</th>
</tr>
</thead>
</table>
| **BBA 1997** | • CAH Program established.  
• Hospitals should operate no more than 15 acute beds and no more than 25 total beds, including swing beds.  
• All patients’ LOS limited to 4 days.  
• Only government and NFP hospitals qualify.  
• Hospitals must be distant from nearest neighboring hospital, at least 35 miles by primary road and 15 by secondary road.  
• States can waive the distance requirement by designating “necessary providers”.
| **BBRA 1999** | • LOS restriction changes to an average of 4 days.  
• States can designate any hospital to be “rural” allowing CAHs to exist in MSAs.  
• FP hospitals allowed to participate.
| **BIPA 2000** | • Payments for MDs “on call” are included in cost-based payments.  
• Cost-based payments for post-acute patiente in swing beds.
| **MMA 2003** | • Inpatient limit increased from 15 to 25 patients.  
• Psychiatric and rehabilitation units are allowed and do not count against the 25 bed limit.  
• Payments are increased to 101 percent of cost.  
• Starting in 2006, states can no longer waive the distance requirement.

**LOS**: Length of Stay  
*Source: MedPac(2005)*
Table 2: Definitions of Rural-Urban Commuting Area Codes

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Metropolitan area core: primary flow within an Urbanized Area (UA)</td>
</tr>
<tr>
<td>2</td>
<td>Metropolitan area high commuting: primary flow 30% or more to UA</td>
</tr>
<tr>
<td>3</td>
<td>Metropolitan area low commuting: primary flow 10% to 30% to UA</td>
</tr>
<tr>
<td>4</td>
<td>Micropolitan area core: primary flow within an Urban Cluster of 10,000 through 49,999</td>
</tr>
<tr>
<td>5</td>
<td>Micropolitan high commuting: primary flow 30% or more to a large UC</td>
</tr>
<tr>
<td>6</td>
<td>Micropolitan low commuting: primary flow 10% to 30% to a large UC</td>
</tr>
<tr>
<td>7</td>
<td>Small town core: primary flow within UC of 2,500 through 9,999</td>
</tr>
<tr>
<td>8</td>
<td>Small town high commuting: primary flow 30% or more to a small UC</td>
</tr>
<tr>
<td>9</td>
<td>Small town low commuting: primary flow 10% through 29% to a small UC</td>
</tr>
<tr>
<td>10</td>
<td>Rural areas: primary flow to tract outside a UA or UC (including self)</td>
</tr>
</tbody>
</table>

Each code has up to 6 subcodes that classify the zip code depending on their percentage flow to Urbanized Areas or Urban Clusters
Table 3: Summary Statistics – Analysis Sample

<table>
<thead>
<tr>
<th></th>
<th>Mean</th>
<th>Std. Dev.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Profits ($1,000)</td>
<td>923.13</td>
<td>2,679.44</td>
</tr>
<tr>
<td>CAH Status</td>
<td>.22</td>
<td>.42</td>
</tr>
<tr>
<td>Not-For-Profit</td>
<td>.51</td>
<td>.50</td>
</tr>
<tr>
<td>Government</td>
<td>.39</td>
<td>.48</td>
</tr>
<tr>
<td>For-Profit</td>
<td>.11</td>
<td>.31</td>
</tr>
<tr>
<td>Beds</td>
<td>52.19</td>
<td>37.60</td>
</tr>
<tr>
<td>$\hat{f}$</td>
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<td>1,884.36</td>
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<tr>
<td>HHI</td>
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<td>.19</td>
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<tr>
<td>$CAH_{Comp}$</td>
<td>.00028</td>
<td>.0014</td>
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<tr>
<td>$EV_{on-Med}^N$</td>
<td>15,176.7</td>
<td>13,700.17</td>
</tr>
<tr>
<td>$EV_{on-Med}^M$</td>
<td>2,817.2</td>
<td>2,256.49</td>
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<tr>
<td>Investment ((\Delta) Beds)</td>
<td>-1.78</td>
<td>8.50</td>
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<tr>
<td>Closure</td>
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<td>.090</td>
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<tr>
<td>N</td>
<td>16,609</td>
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<tr>
<td>Number of Hospitals</td>
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</table>

Table 4: Summary Statistics in 2005 by CAH Status

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<th>CAH</th>
<th>Non-CAH</th>
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<td>Profits ($1,000)</td>
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<td>1,835.1</td>
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<td>Not-For-Profit</td>
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<td>.52</td>
</tr>
<tr>
<td>Government</td>
<td>.49</td>
<td>.32</td>
</tr>
<tr>
<td>For-Profit</td>
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<td>.16</td>
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<td>Beds</td>
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<td>70.17</td>
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<tr>
<td>HHI</td>
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<td>.4485</td>
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<tr>
<td>$EV_{on-Med}^M$</td>
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<td>Investment (Beds)</td>
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<tr>
<td>Closure</td>
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<td>.0081</td>
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<tr>
<td>N</td>
<td>916</td>
<td>984</td>
</tr>
<tr>
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<td>Medicare</td>
<td>S.E.</td>
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<tr>
<td>-------------------</td>
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</tr>
<tr>
<td>Distance</td>
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<td>0.0024</td>
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<tr>
<td>Distance²/100</td>
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</tr>
<tr>
<td>Dist × Urban</td>
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<td>0.0025</td>
</tr>
<tr>
<td>Dist² × Urban</td>
<td>2.96</td>
<td>0.22</td>
</tr>
<tr>
<td>Closest</td>
<td>2.61</td>
<td>0.067</td>
</tr>
<tr>
<td>Closest × Beds</td>
<td>-0.0025</td>
<td>0.00016</td>
</tr>
<tr>
<td>Closest × Urban</td>
<td>-0.49</td>
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<tr>
<td>CAH</td>
<td>-14.68</td>
<td>4.12</td>
</tr>
<tr>
<td>CAH × Closest</td>
<td>12.36</td>
<td>3.85</td>
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<tr>
<td>CAH × Dist</td>
<td>2.61</td>
<td>0.067</td>
</tr>
<tr>
<td>Beds</td>
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<td>0.0014</td>
</tr>
<tr>
<td>Beds²</td>
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<td>0.000020</td>
</tr>
<tr>
<td>Teaching</td>
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<td>0.040</td>
</tr>
<tr>
<td>Closest × Dist</td>
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<td>0.0019</td>
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<tr>
<td>Teach × Dist</td>
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<td>0.00089</td>
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<tr>
<td>Beds × Dist</td>
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<tr>
<td>Likelihood</td>
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Table 6: First-Stage Regression: Profits ($1,000)

<table>
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<tr>
<th>Variable</th>
<th>Estimate</th>
<th>Robust s.e.</th>
<th>t</th>
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<tbody>
<tr>
<td>CAH status</td>
<td>471.42</td>
<td>164.60</td>
<td>2.86</td>
</tr>
<tr>
<td>Beds</td>
<td>19.14</td>
<td>7.58</td>
<td>2.52</td>
</tr>
<tr>
<td>( \hat{f} )</td>
<td>.51</td>
<td>.076</td>
<td>6.61</td>
</tr>
<tr>
<td>( \hat{f}^2 )</td>
<td>.000036</td>
<td>.000015</td>
<td>2.61</td>
</tr>
<tr>
<td>( \hat{f}^3 )</td>
<td>-3.15x10^{-9}</td>
<td>1.67x10^{-9}</td>
<td>-1.89</td>
</tr>
<tr>
<td>HHI</td>
<td>-2278.60</td>
<td>869.22</td>
<td>-2.62</td>
</tr>
<tr>
<td>HHI^2</td>
<td>1928.04</td>
<td>9.03</td>
<td>2.13</td>
</tr>
<tr>
<td>( \hat{f} \ast CAH )</td>
<td>.095</td>
<td>.19</td>
<td>.54</td>
</tr>
<tr>
<td>Vol. Under 65</td>
<td>045</td>
<td>0.0011</td>
<td>3.92</td>
</tr>
<tr>
<td>Vol. Over 65</td>
<td>-.081</td>
<td>0.072</td>
<td>-1.12</td>
</tr>
<tr>
<td>CAH_{comp}</td>
<td>-23,035.20</td>
<td>10,000.12</td>
<td>-2.30</td>
</tr>
<tr>
<td>CAH_{comp}*CAH</td>
<td>27,279.48</td>
<td>17,688.6</td>
<td>1.54</td>
</tr>
<tr>
<td>( R^2 )</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>N</td>
<td>16,609</td>
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Standard errors clustered at the hospital level
Table 7: First-Stage Regression: CAH Conversion

<table>
<thead>
<tr>
<th>Variable</th>
<th>Estimate</th>
<th>Robust s.e.</th>
<th>z</th>
</tr>
</thead>
<tbody>
<tr>
<td>NFP</td>
<td>.90</td>
<td>.23</td>
<td>3.84</td>
</tr>
<tr>
<td>Gov</td>
<td>.78</td>
<td>.23</td>
<td>3.32</td>
</tr>
<tr>
<td>Beds</td>
<td>.015</td>
<td>.014</td>
<td>1.12</td>
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<tr>
<td>Beds$^2$</td>
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<td>.0002</td>
<td>-10.78</td>
</tr>
<tr>
<td>$\hat{f}$</td>
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<td>.33</td>
<td>-.53</td>
</tr>
<tr>
<td>$\hat{f}^2$</td>
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<tr>
<td>$\hat{f}^3$</td>
<td>.002</td>
<td>.002</td>
<td>0.98</td>
</tr>
<tr>
<td>HHI</td>
<td>.45</td>
<td>1.61</td>
<td>.28</td>
</tr>
<tr>
<td>$\hat{f} \times HHI$</td>
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<td>1.27</td>
<td>1.11</td>
</tr>
<tr>
<td>$\hat{f} \times Beds$</td>
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<td>.0041</td>
<td>-2.27</td>
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<td>0.000016</td>
<td>3.43</td>
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<td>-2.85</td>
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<tr>
<td>CAH Comp</td>
<td>27.0</td>
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</tr>
<tr>
<td>$x$</td>
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<tr>
<td>Constant</td>
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<td>.54</td>
<td>-2.47</td>
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</tbody>
</table>

Log Likelihood: -1,895.5
N: 11,155

Standard errors clustered at the hospital level
<table>
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<tr>
<th>Variable</th>
<th>Estimate</th>
<th>Robust s.e.</th>
<th>z</th>
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</thead>
<tbody>
<tr>
<td>NFP</td>
<td>.90</td>
<td>.23</td>
<td>3.84</td>
</tr>
<tr>
<td>Gov</td>
<td>.78</td>
<td>.23</td>
<td>3.32</td>
</tr>
<tr>
<td>CAH status</td>
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</tr>
<tr>
<td>CAH status*Beds</td>
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<td>-.96</td>
</tr>
<tr>
<td>( \hat{f} )</td>
<td>-.045</td>
<td>.18</td>
<td>-.25</td>
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<tr>
<td>( \hat{f}^2 )</td>
<td>.0041</td>
<td>.58</td>
<td>.71</td>
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<tr>
<td>( \hat{f}^3 )</td>
<td>-.00027</td>
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<td>-0.58</td>
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<tr>
<td>HHI</td>
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<td>-.37</td>
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<td>( \hat{f} \times \text{HHI} )</td>
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<td>.73</td>
<td>.22</td>
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<td>( \hat{f} \times \text{Beds} )</td>
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<td>.00097</td>
<td>.48</td>
</tr>
<tr>
<td>Vol. Under 65</td>
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<td>0.000013</td>
<td>1.27</td>
</tr>
<tr>
<td>Vol. Over 65</td>
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<td>0.000084</td>
<td>-.28</td>
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<tr>
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<td>.18</td>
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<td>-2.47</td>
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<tr>
<td>( \bar{x} )</td>
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<td>.15</td>
<td>85.08</td>
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<tr>
<td>( \sigma_x )</td>
<td>19.10</td>
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<td>40.48</td>
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<td>N</td>
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Table 9: Parameter Estimates Dynamic Oligopoly Equilibrium

<table>
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<tbody>
<tr>
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<td>(26)</td>
</tr>
<tr>
<td>$\alpha_{Gov}$</td>
<td>2984</td>
<td>(1616)</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>.010</td>
<td>(.004)</td>
</tr>
</tbody>
</table>

$\alpha_{NFP}$ = \frac{v}{-76 \pm (26)}$

$\alpha_{Gov}$ = \frac{p}{2984 \pm (1616)}$

$1 \{x > 0\} = \frac{x}{-200 \pm (100)}$

$1 \{x > 0\}x = \frac{3414}{(1105)}$

$1 \{x > 0\}x^2 = \frac{.480}{(.311)}$

$1 \{x < 0\} = \frac{1.803}{(1105)}$

$1 \{x < 0\}x = \frac{-2363}{(717)}$

$1 \{x < 0\}x^2 = \frac{20.5}{(15.3)}$

$1 \{x > 0\}x\sigma = \frac{1090}{(377)}$

$1 \{x < 0\}x\sigma = \frac{1558}{(561)}$